

**SUPPORTING INFORMATION**

**Spatial resolution of coherent cathodoluminescence  
super-resolution microscopy**

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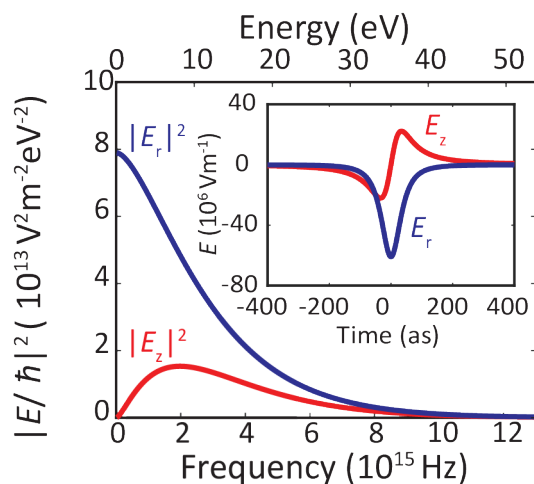
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(5 pages and 2 figures)

### 1) Electron excitation energy spectrum

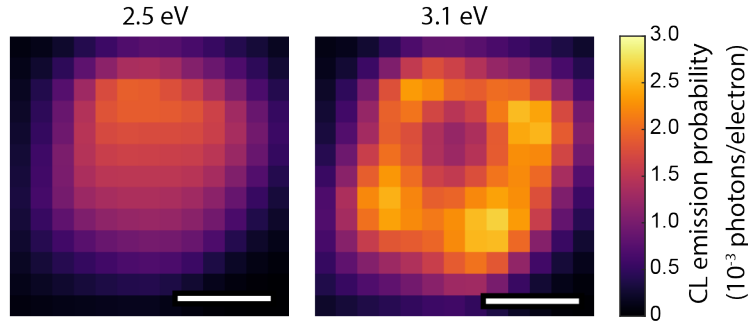
Figure S1 shows the time evolution of the radial and axial electric field intensity at a fixed position 5 nm away from a trajectory of a 30 keV electron. The field components form a single oscillation in a period of several 100 attoseconds. The corresponding energy spectrum spans a broad range from 0 to ~40 eV: the spectrum monotonously decreases with energy for the radial component while for radial component it peaks at ~8 eV. This broad spectrum makes high-energy electrons an effective broadband source of excitation in the optical spectral range. The plasmon resonances in the 2.2-3.2 eV spectral range (see Figure 1a) can be readily excited by the 30 keV electron.



**Figure S1.** Inset: Time evolution of the radial ( $E_r$ ) and axial ( $E_z$ ) electric field intensity 5 nm away from the trajectory of a 30 keV electron in vacuum. Main panel: Fourier transform showing the corresponding energy spectra.

### 2) SEM/CL experiments

CL experiments were performed using a Thermo Fisher/FEI Quanta 650 FEG SEM equipped with a Delmic SPARC CL collection and analysis system equipped with a photomultiplier tube in combination with a bandpass filter, and Czerny-Turner spectrometer equipped with a CCD array detector. The typical beam current in the CL measurements was 0.5-5nA. CL spectra were normalized using measurements and calculations of transition radiation on an Al surface.<sup>1</sup> For all spectral measurements we collect a substrate reference and subtract it from the data. CL line scans were taken using a Hamamatsu H10721-20 photomultiplier tube, sensitive in the 1.3-5.4 eV spectral range using 1 nm steps. Coarse spectral CL maps were taken with a 11 nm pixel size. Figure S2 shows maps of the dipolar and corner modes at 2.5 eV and 3.1 eV, respectively. Secondary electrons were collected with an Everhart-Thornley detector that is aligned with optical axis of the paraboloid mirror and faces the open end of the mirror. The HAADF-STEM image in Figure 1b is taken using a Thermo Fisher/FEI Verios G4 XHR SEM.



**Figure S2.** Spatial CL maps (30 keV) of a 70 nm Ag nanocube at 2.5 eV and 3.1 eV, using a collection bandwidth of 40 nm. Scale bar = 50 nm.

### 3) Ag nanocube synthesis

Single-crystalline Ag nanocubes were made using chemical synthesis originally described in Ref. 2 and drop-cast onto a 15-nm-thick low-stress Si<sub>3</sub>N<sub>4</sub> membrane (Silchem) to create a near-symmetric dielectric environment for the nanocubes and avoid unwanted incoherent CL from the substrate. The particle sizes are in the range 75 ± 5 nm. Prior to the CL measurements polyvinylpyrrolidone ligands were removed from the Ag nanocubes using sodium borohydride to minimize the build-up of carbon contamination during electron irradiation.

### 4) CASINO simulations

Simulations were done for a 70 nm Ag cube without substrate. A total of 10<sup>5</sup> primary electron trajectories was simulated for each incident beam position for 10 keV and 30 keV. We used Ag density: 10.5 g/cm<sup>3</sup>, Ag bulk plasmon energy 3.78 eV, and Ag work function 4.64 eV.

### 5) Analytical SE model

The analytical model for  $I_{\text{cube}}(x)$  in Eq. (1) has three factors:

#### a) $C_{\text{SE}}(x', x)$

The SE generation density  $C_{\text{SE}}(x', x)$  as a function of position  $x'$  for an electron incident at  $x$  in a vertical plane centered in the Ag nanocube, integrated over the nanocube height, is modeled using a Gaussian distribution:

$$C_{\text{SE}}(x', x) = \begin{cases} \frac{N_{\text{SE}}}{\sigma_{\text{SE}}\sqrt{2\pi}} \exp\left(-\frac{(x'-x)^2}{2\sigma_{\text{SE}}^2}\right) & \frac{-D}{2} < x' < \frac{D}{2} \text{ and } \frac{-D}{2} < x < \frac{D}{2} \\ 0 & \text{elsewhere} \end{cases} \quad (\text{S1})$$

with  $N_{\text{SE}}$  the number of secondary electrons generated per primary electron,  $\sigma_{\text{SE}}$  the standard deviation, and  $D$  the nanocube size.

#### b) $P_{\text{esc}}(x')$

The probability  $P_{\text{esc}}(x')$  that a SE generated at a position  $x'$  escapes from the nanocube (integrated over the nanocube height) so it can be detected is modeled using:

$$P_{\text{esc}}(x') = P_{\text{side}}(x') + P_{\text{top}} \quad (\text{S2})$$

with  $P_{\text{top}}$  the probability for SEs escaping from the top, which we assume to be independent of  $x'$ , and  $P_{\text{side}}(x')$  the probability for SEs to escape from the side facets which is modeled using:

$$P_{\text{side}}(x', \sigma_{\text{esc}}, D) = \int_{-\frac{D}{2}}^{\infty} P_s \exp\left(-\frac{(x' + \frac{D}{2})^2}{2\sigma_{\text{esc}}^2}\right) + \int_{-\infty}^{\frac{D}{2}} P_s \exp\left(-\frac{(x' - \frac{D}{2})^2}{2\sigma_{\text{esc}}^2}\right) \quad (\text{S3})$$

with  $\sigma_{\text{esc}}$  the effective electron escape depth from the cube and  $P_s$  a scaling factor.

c)  $B(x, \sigma_{\text{beam}})$

The integral over  $C_{\text{SE}}(x', x)P_{\text{esc}}(x')$  in Eq. (1) is convolved with the beam profile that is modeled using a Gaussian distribution:

$$B(x, \sigma_{\text{beam}}) = \frac{1}{\sigma_{\text{beam}}\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma_{\text{beam}}^2}\right) \quad (\text{S4})$$

with  $\sigma_{\text{beam}}$  the standard deviation. We use effective beam widths of 2 nm and 12 nm FWHM, corresponding to  $\sigma_{\text{beam}} = 0.85$  nm and  $\sigma_{\text{beam}} = 5.1$  nm.

The simulated SE coefficient as a function of beam position in Figures 2b,d was then fitted with Eqn. (1), using as free parameters the width of the SE distribution  $\sigma_{\text{SE}}$ , the escape depth  $\sigma_{\text{esc}}$  and the product  $N_{\text{SE}}P_s$ . The resulting function  $N_{\text{SE}}P_{\text{esc}}(x')$  is plotted in Figures 2a,c for the two beam widths and beam energies. At each energy and beam width similar graphs  $P_{\text{esc}}(x')$  for values for  $P_{\text{top}}$  and  $P_s$  are found for the fits for the two different beam widths ( $\sigma_b$ ), as expected.

As described in the main text the analytical model for  $I_{\text{cube}}(x)$  in Eq. (1) was also used to fit the SE line profiles with the beam width as a free parameter. A beam width of  $\sigma_{\text{beam}} = 5-6$  nm was consistently found for the best beam alignment conditions.

#### 6) MNPBEM simulations

MNPBEM calculations were made for Ag nanocubes in vacuum using a cubic mesh with a size of 3.5 nm. Particles were marginally rounded (default value). Optical constants for Ag were taken from Ref. 3 and the beam width was 0.2 nm. Using the retarded MNPBEM beam solver the angle-dependent radiation patterns were derived from the calculated surface charges and currents. The CL spectrum was then obtained by collecting all emission over all angles.

#### 7) Analytical CL model

The CL signal across the nanocube is modeled using the following qualitative model:

$$I_{\text{CL}}(x, L, a, b, D) = \begin{cases} (a + b) \exp\left(\frac{x + \frac{D}{2}}{L}\right) & x < -\frac{D}{2} \\ a + b \left[ \exp\left(-\frac{x - \frac{D}{2}}{L}\right) + \exp\left(\frac{x + \frac{D}{2}}{L}\right) \right] & -\frac{D}{2} < x < \frac{D}{2} \\ (a + b) \exp\left(-\frac{x - \frac{D}{2}}{L}\right) & x > \frac{D}{2} \end{cases} \quad (\text{S5})$$

This equation reflects the CL plateau observed the particle top with amplitude  $a$ , the exponential decay outside the cube ( $x < -D/2$  and  $x > D/2$ ) with amplitude  $(a+b)$  at the particle edge and characteristic decay length  $L$ , and the two exponential tails on top of the particle, with amplitude  $b$  and the same characteristic decay length  $L$ . Similar to the case for  $I_{\text{cube}}(x)$  above we convolute  $I_{\text{CL}}(x)$  with the Gaussian distribution Eq. S4 that reflects the effective beam width. The beam widths found from the fit of the CL profiles are  $\sigma_b = 5$ - $6$  nm for the best beam alignment conditions, and are linearly correlated with the beam widths derived from the fits of the SE data.

## References

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2. Tao, A., Sinsersuksakul, P. & Yang, P. Polyhedral silver nanocrystals with distinct scattering signatures. *Angew. Chemie - Int. Ed.* **45**, 4597–4601 (2006).
3. Johnson, P.B., and Christy, R. W. Optical constants of the noble metals. *Phys. Rev. B* **6**, 4370 (1972).